

陳又瑄Chenys

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傳送日期: 2013年12月10日 下午 11:54
主旨: Colloquium 演講 (by 張德健_
Dear Ms. Chen,

Please announce the following talk.

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時間: 12月19日 下午 1:10-2:00

Speaker: 張德健教授(Georgetown University)

題目 : Heat Kernels for a family of Grushin operators

摘要:

\begin{abstract}

In this talk, we construct the heat kernel for the second-order operator

$$\Delta_X = \frac{1}{2} \sum_{k=1}^n \left(\frac{\partial}{\partial x_k} \right)^2 + \frac{1}{2} \sum_{k=1}^n \left(\frac{\partial}{\partial x_k} \right)^2 + \frac{1}{2} \sum_{k=1}^n \left(\frac{\partial}{\partial y_k} \right)^2$$
 with $m_k \in \mathbb{N}$,

which is a degenerate

elliptic operator. Obviously, this operator is closely related to the Grushin operator

$$L_G = \frac{1}{2} \left(\frac{\partial}{\partial x} \right)^2 + \frac{1}{2} \left(x^m \frac{\partial}{\partial y} \right)^2$$
 with $m \in \mathbb{N}$.

In this paper, we first give a complete description of the geometry induced by the operator L_G . More precisely, given any two points in the space, the number of geodesics and the lengths of the geodesics are calculated. Then we find modified complex action functions and show that the critical values of this function will recover the lengths of the corresponding geodesics. We also find the volume element by solving a generalized transport equation. Finally, the formula for the heat kernel of the diffusion operator $\frac{\partial}{\partial t} - \Delta_X$ is obtained. The formula involves an integral of a product between the volume function and an exponential term.

\end{abstract}

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Thank you,

Best,

Hsin-Yuan

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